

Roll No.

2011

B. E. 3rd Sem. (I. T.)

Examination – December, 2011

DISCRETE STRUCTURE

Paper : CSE-203-E

Time : Three hours]

[Maximum Marks : 100

Before answering the questions, candidates should ensure that they have been supplied the correct and complete question paper. No complaint in this regard, will be entertained after examination.

Note : Attempt *five* questions in total.

1. Explain the following terms with suitable examples :

(i) Set,

(ii) Classes of Sets,

(iii) Power Sets,

(iv) Types of Relation,

(v) Partial Ordering Relation.

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2. Define propositions, tautologies, contradictions and hence prove that the following propositions are tautology :

(i) $p \vee \sim p$

(ii) $\sim(p \wedge q) \vee q$

(iii) $p \Rightarrow (p \vee q)$

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3. (a) Explain permutations and combination and hence find in how many ways a committee of 3 faculty members and two students be selected from 7 faculty members and 8 students.

12

(b) Define AP, GP and AG series with examples. Also write the formula for sum of n terms in AP, GP, AG series.

8

4. (a) Solve the recurrence relation :

$$a_r + 5 a_{r-1} + 6 a_{r-2} = 3r^2 - 2r + 1. \quad 10$$

(b) Solve the recurrence relation :

$$a_{r+2} - 3 a_{r+1} + 2 a_r = 0 \quad \text{by the method of} \\ \text{generating functions with the initial conditions} \\ a_0 = 2, a_1 = 3. \quad 10$$

5. Discuss about the following terms with examples :

(i) Groups and Rings,

(ii) Homomorphism and Isomorphism in Groups and Rings.

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6. Write note on the following :

- (i) Directed and Undirected Graphs,
- (ii) Homomorphic Graphs,
- (iii) Cut points and Bridges,
- (iv) Paths and Circuit.

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7. (a) How do we determine whether there is a Hamiltonian circuit in a graph or not ?

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(b) State and prove Lagrange's Theorem.

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8. (a) What is a binary search tree ? Give examples.

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(b) Let $f(x) = x - 1$ and $g(x) = x^2$, find :

(i) $g \circ f(-2)$

(ii) $f \circ g(-2)$

5

(c) Define Lattice with examples.

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